

An alternate expression for this matrix product is

$$M^n = \begin{bmatrix} 1/2C_n(2A) & BS_{n-1}(2A) \\ CS_{n-1}(2A) & 1/2C_n(2A) \end{bmatrix}. \quad (14)$$

$C_n(2A)$ and $S_{n-1}(2A)$ are Chebyshev polynomials of the first and second kind normalized to $2A$ rather than A as in (13). Term-by-term identification of (13) and (14) serves to define the Chebyshev polynomials C_n and S_{n-1} in terms of Chebyshev polynomials T_n and U_{n-1} . The Chebyshev polynomials $C_n(x)$ and $S_n(x)$ are available [2] for $n=2(1)12$ (*i.e.*, from 2 to 12 in steps of one) for $x=0(0.001)2$ to 12 decimal places. In this reference $U_{n-1}(x)$ is employed where $U_n(x)$ is usually found [4], [5].

A useful quantity for reflection loss and the resulting standing-wave ratio of a periodic transmission line structure is the equivalent susceptance B_{eq} which would give the same VSWR or insertion loss in a unity impedance line. It is found by $jB_{eq}=B-C$ (15) for one stage or $jB_{eq}=(B-C)S_{n-1}(2A)$ (16) for n stages; the relation to voltage standing-wave ratio r is

$$B_{eq} = \frac{r-1}{\sqrt{r}} \quad (17)$$

and to power insertion loss is

$$L = 1 + \frac{B_{eq}^2}{4}. \quad (18)$$

These relations are valid in both the pass band $|A| \leq 1$ and the stop band $|A| \geq 1$.

JOHN REED
Raytheon Co.
Wayland, Mass.

BIBLIOGRAPHY

- [1] J. Reed, "The multiple branch waveguide coupler," *IRE TRANS. ON MICROWAVE THEORY AND TECHNIQUES*, vol. MTT-6, pp. 398-403, October, 1958.
- [2] "Tables of Chebyshev Polynomials ($S_n(x)$ and $C_n(x)$)," Natl. Bur. of Standards Appl. Math. Ser. No. 9, U. S. Govt. Printing Office; Washington, D. C.
- [3] A. J. Simmons, "Phase shift by periodic loading of waveguide and its application to broad-band circular polarization," *IRE TRANS. ON MICROWAVE THEORY AND TECHNIQUES*, vol. MTT-3, pp. 18-21; December, 1955.
- [4] W. L. Pritchard, "Quarter wave coupled waveguide filters," *J. Appl. Phys.*, vol. 18, pp. 862-872; October, 1957.
- [5] M. C. Pease, "The iterated network and its application to differentiators," *Proc. IRE*, vol. 40, pp. 709-711, June, 1952.

X-Band Diode Limiting*

Broad-band, matched, low power, instantaneous, passive, X -band diode limiting has been demonstrated. The limiter, which uses standard microwave components, is an outgrowth of point contact germanium diode microwave switch research. In fact, the hybrid-tee switch¹ makes a very good nar-

row-band limiter under the condition of zero bias voltage on the crystals (biasing terminals short circuited). The output power under these conditions is limited to 0.5 mw² for incident power up to 30 mw, deduced from Fig. 9 of Garver, *et al.*³ However, the bandwidth of the hybrid-tee switch when used as a limiter is insufficient for many applications such as limiting the amplitude of a 0.2- μ sec magnetron pulse or flattening a frequency-modulated klystron mode.

From our experience with the hybrid-tee switch, we concluded that any diode switch providing high isolation with diode conduction and low insertion loss with nonconduction will function passively as a limiter. Low RF power does not cause significant diode conduction, while high RF power results in conduction which changes the diode impedance, causing increasing attenuation. Thus a more broad-band switch is needed that provides high isolation with the diode in the conducting state.

Although the basic X -band diode switch using a point contact germanium diode such as the 1N263 is broad-band, it provides high isolation in the nonconduction state, and therefore does not fulfill the above criteria. In fact, with its biasing terminals short-circuited, this switch acts as an expander.

Using a technique developed by Sweet,⁴ it is possible to make a broad-band switch having isolation with diode conduction and which is matched as well for all biases on the diode. Fig. 1 shows the block diagram for using Sweet's technique at X -band. If both arms containing diodes are identical reflectors, the properties of the 90° , 3-db coupler are such that the phases of the reflected waves add at the output arm and cancel at the input arm; thus all power reflected from the diodes comes out the output arm, and the input arm always appears matched. Using slide screw tuners next to the diodes, a switch has been made giving isolation greater than 20 db over a 400-Mc bandwidth with an insertion loss of 0.7 db or less. The isolation is greater than 30 db over a 150-Mc bandwidth. This is much better than the hybrid-tee switch isolation of greater than 30 db over a 20-Mc bandwidth.

When the short-slot hybrid junction switch with two diodes is used as a limiter, however, the output does not remain constant with increasing incident power but increases slightly. The action could be better described as compression. Better limiting is obtained by using power sensitive tuners behind the diodes instead of fixed tuners. A second 1N263 space $\frac{1}{4} \lambda_g$ from the first has been found to give the flattest limiting. As shown in Fig. 2, the output at the center frequency is limited to $0.43 \text{ mw} \pm 0.1 \text{ db}$ for all incident power from 2 mw to 200 mw.⁴ For pulsed power up to 10 watts peak, the output increases to 2 mw peak. Pulse energy greater than 1 watt μ sec permanently damages the diodes so that the low power insertion loss of the limiter is increased above its

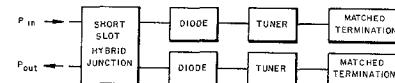


Fig. 1—Block diagram for making matched diode switch.

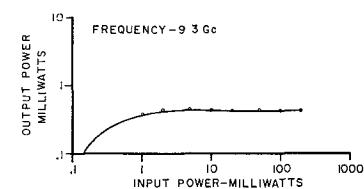


Fig. 2—Limiting using 4 1N263's and a short-slot hybrid junction.

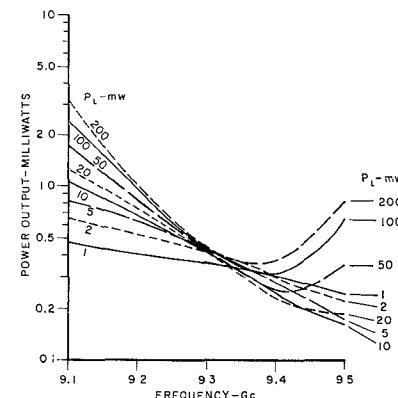


Fig. 3—Frequency dependence of limiting with diodes at $\frac{1}{4} \lambda_g$ spacing.

typical value of 0.7 db.

The frequency dependence of the limiting for $\frac{1}{4} \lambda_g$ spacing is shown in Fig. 3. For input power ranging from 2 mw to 200 mw, the output power is $0.45 \text{ mw} \pm 1 \text{ db}$ over a 60-Mc bandwidth, and $\pm 2 \text{ db}$ over a 120-Mc bandwidth. This limiter has been successfully used for suppressing the unwanted AM from an FM klystron.⁵ Unless fringing effects forbid it, flat limiting should occur at one quarter wavelength between diodes. With the smaller spacing it is anticipated that only the abscissa of Fig. 3 would be changed, so that the data for 9.1 Gc would occur at 8.7 Gc and the data for 9.5 Gc would occur at 9.9 Gc, *i.e.*, the bandwidth should be tripled. To place the diodes one quarter-wavelength apart it will be necessary to redesign the diode mount so that it is smaller. Since the limiter does not require external biasing terminals or RF chokes, the dc shorts can be built into the diode mounts.

R. V. GARVER
D. Y. TSENG
Ordnance Corps.
Diamond Ordnance Fuze Labs.
Washington, D. C.

* Received by the PGMTT, January 5, 1961.

¹ R. V. Garver, E. G. Spencer, and M. A. Harper, "Microwave semiconductor switching techniques," *IRE TRANS. ON MICROWAVE THEORY AND TECHNIQUES*, vol. MTT-6, pp. 378-383; October, 1958. (See especially page 381.)

² Open-circuit bias terminals cause limiting at a higher output power level.

³ L. Sweet, "Instantaneous Automatic Gain Control (IAGC) Techniques for Crystal Video Receivers," PRD Final Rept. 4.13, Contract No. AF 30(602)-1434/Proj. No. 4505, Task No. 45215, ASTIA AD 148728; December 1, 1957.

⁴ To obtain such flat output, it was necessary to use selected diodes. Diodes picked at random will give about 1 db variation in output. The characteristics were also slightly affected by diode rotation and seating.

⁵ J. Samuel, "Diamond Ordnance Fuze Laboratories Workbook No. 1955." Unpublished.